

HPL overview

WIDE kick-off meeting

Siena

September 26-27, 2008

Honeywell

- **About the partner**
 - Honeywell
 - HPL team

- **R&D in WIDE area**
 - System identification
 - Decentralized optimization
 - Wireless control networks

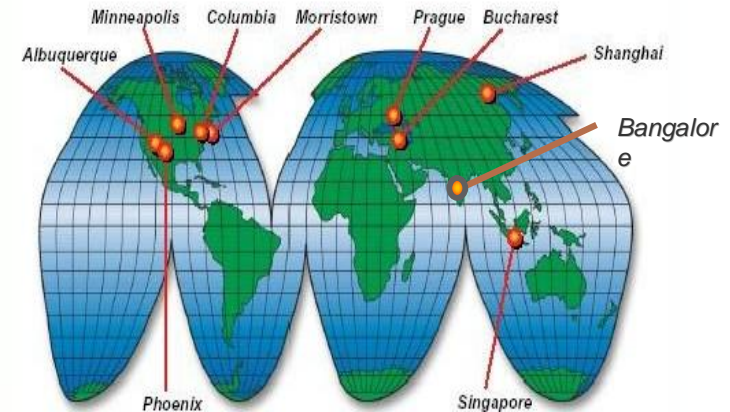
Honeywell International

- 122,000 employees
- over 100 countries
- A *Fortune* 100 company – 2007 sales \$34.6B
- 1000+ APC/RTO applications
(Profit Suite, UES – developed in HPL)

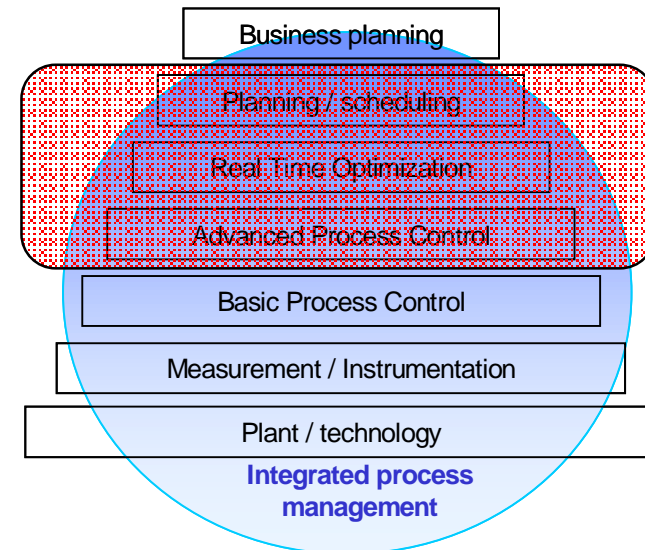
Honeywell's Research Organization

- \$750M Spent Annually on R&D
- R&D supporting all business segments (ACS, AERO, SM, TS)
- ACS and AERO Labs
 - HQ'd in Minneapolis, MN
- Prague lab – branch of ACS AT lab
 - 30 employee, MSc/PhD level
 - PCO / DCT group
 - Control & optimization + domain knowledge
 - Algorithmic development → software prototyping → pilot testing
 - Productization / NPI (Bangalore)

Honeywell research organization



HPL PCO group scope



HPL alignment – ACS AT lab

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ACS Profile

\$12.5B Revenue

More than 55,000 Employees

Process Solutions
\$1.8B

Building Solutions
\$1.9B

Sensing and Control
\$0.8B

ECC
\$2.1B

Security
\$1.8B

Life Safety
\$0.9B

Process Controls



Distributed Control



OneWireless

Buildings



Instant Alert



Speed and Position Sensors



Accelerometers

Pressure Sensors



Thermostats



Building Automation



Gas Valves

Water Control



Motion / Human Presence Sensors



CCTV/ DVR User Interfaces



Control Systems



Fire/Smoke Sensors



System Panels



Home Medical Care



HPL WIDE related activities

HPL WIDE team



- **Vladimír Havlena**
 - MPC, bayesian/grey box ID
- **Lubomír Baramov**
 - Decentralized MPC / optimization / estimation
 - WP3 leader
- **Daniel Pachner**
 - Stochastic MPC, cautious optimization, NL identificaiton
- **Jaroslav Pekař**
 - MPC, modeling
- **Pavel Trnka**
 - Subspace identification, WCN (resource allocation)
- **Jiří Findejs + sw developer team**
 - SW development, prototyping
 - WP5 implementation support

R&D in WIDE area

**Subspace identification
method for MPC**

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Objective

- Subspace identification methods (SIM) tools for industrial applications of MPC, grey box modeling

Results

- SIM “formal algebraic methods without direct interpretation ...” → interpretation of SIM as weighted multi-step predictor
- Elimination of causality problems and over-parameterization of standard algorithm
- Bayesian interpretation → incorporation of prior information to SIM

Causality and Over-parameterization issues

Core SIM data equation

$$Y_f = \Gamma X_f + HU_f = \underbrace{LW_p}_{\text{Past data}} + \underbrace{HU_f}_{\text{Future inputs}}$$

$$H = \begin{bmatrix} h_0 & & & 0 \\ h_1 & h_0 & & \\ \mathbf{O} & \mathbf{O} & \mathbf{O} & \\ h_{i-1} & \mathbf{O} & \mathbf{O} & h_0 \end{bmatrix}$$

Enforcing H structure in estimation of L and H (S4ID – H full !!)

- formula for matrix product vectorization

$$vec(AB) = (B^T \otimes I)vec(A)$$

- unique H parameters h_0, \dots, h_i

$$vec(H) = N \begin{bmatrix} h_0 \\ \mathbf{M} \\ h_{i-1} \end{bmatrix}$$



$$vec(Y_f) = \underbrace{\left(\begin{bmatrix} W_p^T & U_f^T \end{bmatrix} \otimes I \right) \begin{bmatrix} I & 0 \\ 0 & N \end{bmatrix}}_{\text{Data Reorganization}} \begin{bmatrix} \overline{vec L} \\ h_0 \\ \mathbf{M} \\ h_{i-1} \end{bmatrix}$$

- L structure still to be enforced (rank + consistency with H)

SWLRA of block Hankel matrices

$$\text{vec}(Y_f) = ((W_p^T \quad U_f^T) \otimes I_x) \begin{pmatrix} I_r & 0 \\ 0 & H \end{pmatrix} \begin{pmatrix} q_{kf} \\ q_h \end{pmatrix} = Zq$$

Optimal solution of realization problem

- Keep prior info in the realization step

$$\min_{A,B,C,D} \begin{pmatrix} h_0 - D \\ h_1 - CB \\ \mathbf{M} \\ h_{k-1} - CA^{k-2}B \end{pmatrix}^T P_h^{-1} \begin{pmatrix} h_0 - D \\ h_1 - CB \\ \mathbf{M} \\ h_{k-1} - CA^{k-2}B \end{pmatrix}$$

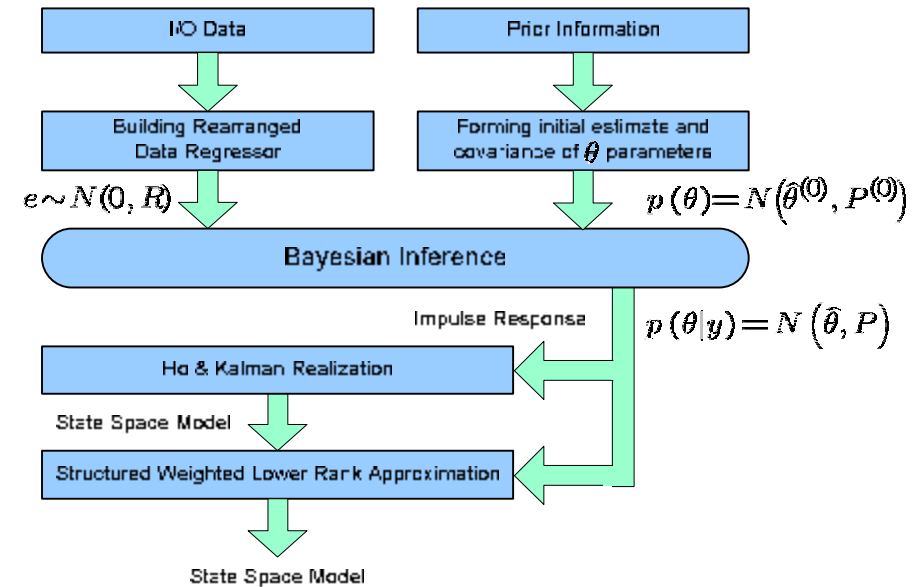
- Approach:

block Hankel matrix H of rank n equivalent to s. s. model of n -th order

$$H = \Gamma_i \Delta_i, \quad \Gamma_i = \begin{pmatrix} C \\ CA \\ \mathbf{M} \\ CA^{i-1} \end{pmatrix}, \quad \Delta_i = (B \quad AB \quad \mathbf{K} \quad A^{i-1}B).$$

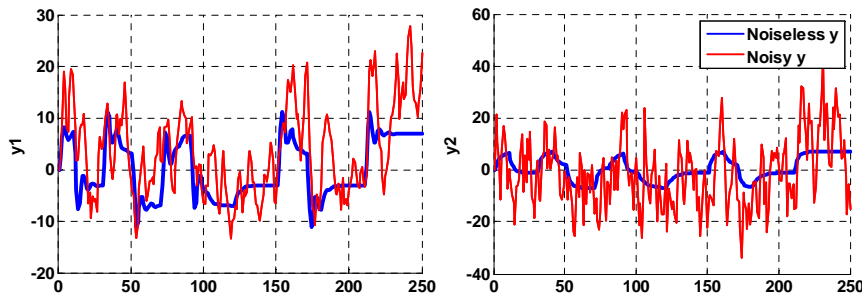
- Solution = SWLRA

- for scalar Hankel matrices solution exists
- solution for MISO – algorithm published (does not converge)
- solution for MIMO – new results

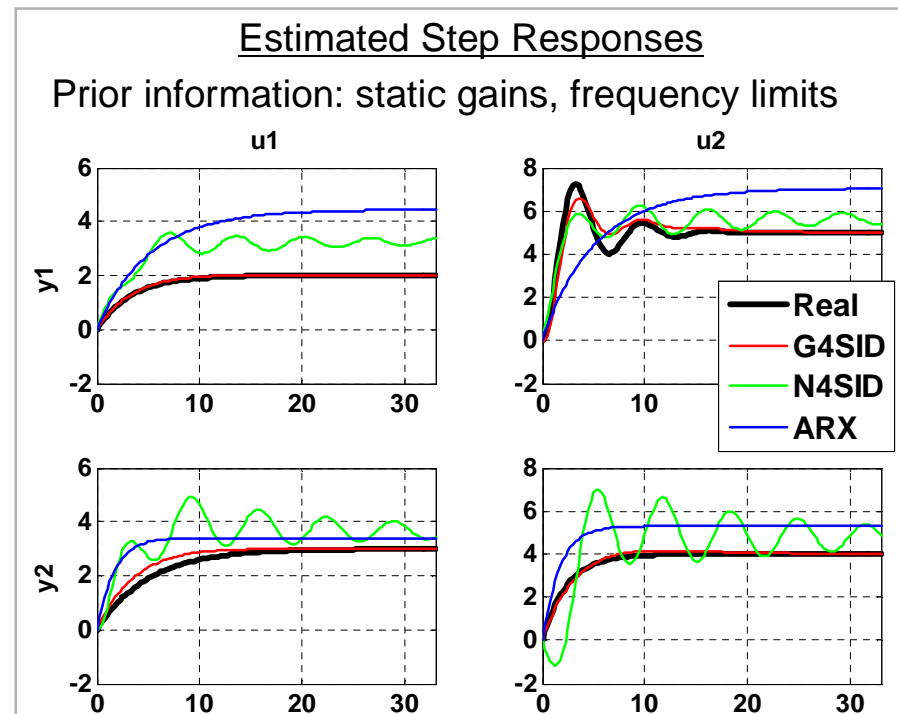


SIM Incorporating Prior Information

- 2 inputs / 2 outputs system of 5th order
- Additive **colored noise**
(multistep predictor equivalent to repeated single-step predictions ?)

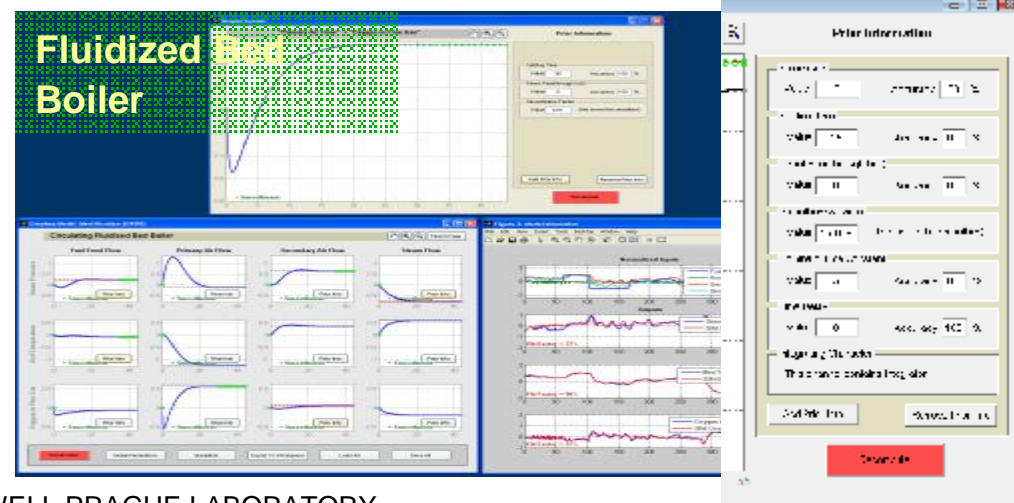


Fit Factor to Noiseless Measurements	Greybox 4SID	85%	91%
	Standard 4SID	71%	39%
	ARX	38%	63%



Problem with industrial applications of APC/RTO = PEOPLE

- MATLAB tool
- Template solution concept
 - Fixed structure (MV, DV, CV)
 - Fixed prior info
 - Parameterized by data



Decentralized Steam Plant Optimization

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Price Coordination Method

- **Two-level iterative scheme**

- Decomposition – set of interconnected blocks
- Prices assigned to interconnected inputs and outputs
- Primary task

$$\hat{\mathbf{x}} = \arg \max_{\mathbf{x}} L^{pc} = \arg \max_{\mathbf{x}} \sum_{i=1}^N Q_i(\mathbf{x}_i) - \langle \boldsymbol{\lambda}_i^T, \mathbf{x}_i^i \rangle + \langle \boldsymbol{\mu}_i^T, \mathbf{y}_i \rangle$$

$$\mathbf{m}_i = \sum_{j=1}^N h_{ji} \mathbf{l}_j, \mathbf{y}_i = f(\mathbf{x}_i)$$

- Dual task (coordinator level)

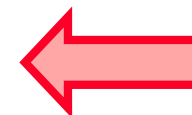
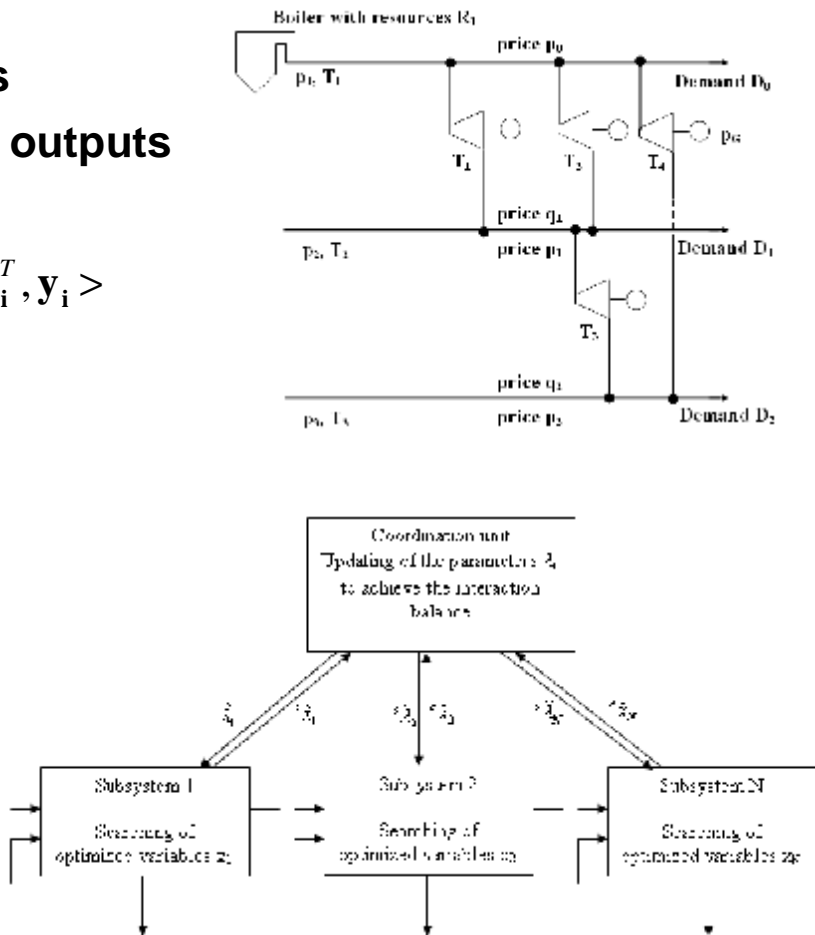
$$\hat{\boldsymbol{\lambda}} = \arg \left\{ \min_{\boldsymbol{\lambda}} \left\{ \max_{\mathbf{x}} L^{pc}(\boldsymbol{\lambda}, \mathbf{x}) \right\} \right\}$$

w update of prices $\boldsymbol{\lambda}$ to ensure balance

$$\mathbf{d} = \hat{\mathbf{x}}(\hat{\boldsymbol{\lambda}}) - \mathbf{B}\hat{\mathbf{y}}(\hat{\boldsymbol{\lambda}}) = 0$$

- **Solution of dual task**

- steepest descent
- Newton method
 - w Hessian evaluated numerically in each iteration
 - w singular Hessian → to be solved ... ; method fast but unreliable
- **modern mp-QP insight (for QP primary task)**
 - w Hessian changes during localization of optimum (a set of polytopes)



- Eliminate the disadvantages of Newton method (Hessian singularity, step length)

- Explicit solution of primary task

- mp-QP optimization problem (primary task)

$$\max_{\mathbf{x}_k} \mathbf{x}_k^T \mathbf{S}_k \mathbf{x}_k + \lambda_k^T \mathbf{M}_k \mathbf{x}_k + \mathbf{p}_k^T \mathbf{x}_k + q_k \quad \mathbf{A}_k \mathbf{x}_k \leq \mathbf{b}_k, \quad k = 1, \dots, N$$

- solution in form of a PWA function of λ_k (for each subsystem)

$$\hat{\mathbf{x}}_k(\lambda) = \mathbf{K}_k^j \lambda + \mathbf{l}_k^j, \quad j = 1, \dots, m$$

w valid in polytope P_j described by

$$\mathbf{G}_k^j \lambda \leq \mathbf{h}_k^j$$

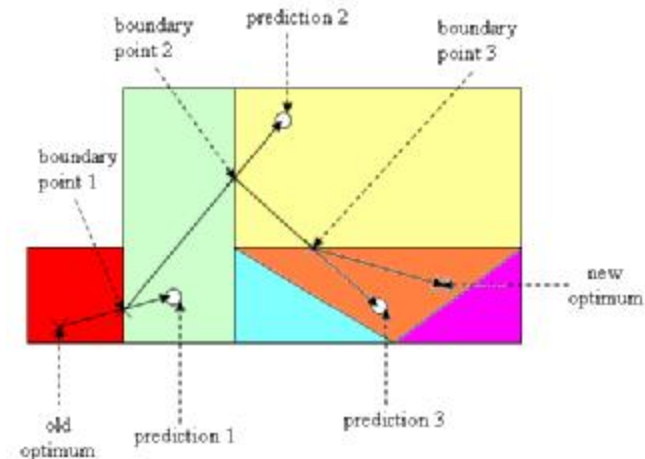
w polytopes of different dimensions (depends on $\dim(\lambda_k)$)

Method Based on mp-QP

- **partitioning of λ – space into set of polytopes**
 - each polytope with singular or regular Hessian
- **dual task: minimization of discoordination**
 - transitions from one polytope to another
 - using “correct” Hessian (K_{BAL}) valid in particular polytope
- **advantages of algorithm**
 - no overshoots
 - fast convergence
 - Hessian known before optimization

$$\mathbf{d} = \hat{\mathbf{x}}(\hat{\lambda}) - \mathbf{B}\hat{\mathbf{y}}(\hat{\lambda})$$

$$\mathbf{d} = \mathbf{K}_{BAL}\hat{\lambda}$$



Method Based on mp-QP

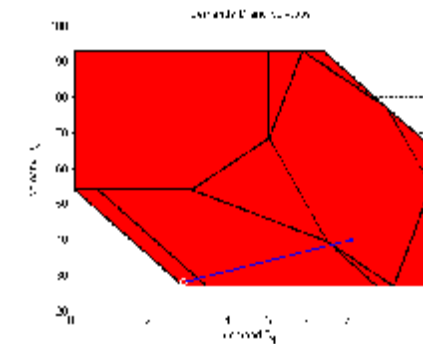
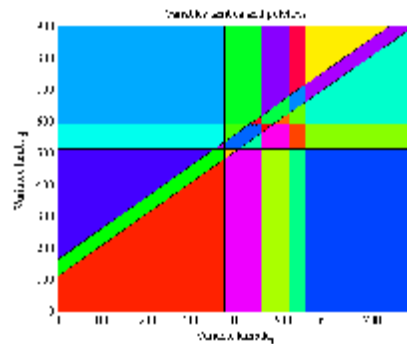
- singular Hessian problem

- detailed analysis of polytopes in λ -space and D-space
- optimum is always located in polytopes with regular Hessian
- only polytopes with $\text{rank}(H) \geq n-1$ need to be traversed

$$\mathbf{d} = \hat{\mathbf{x}}(\hat{\lambda}) - \mathbf{H}\hat{\mathbf{y}}(\hat{\lambda})$$

$$\mathbf{d} = \mathbf{K}_{\text{BAL}} \hat{\lambda}$$

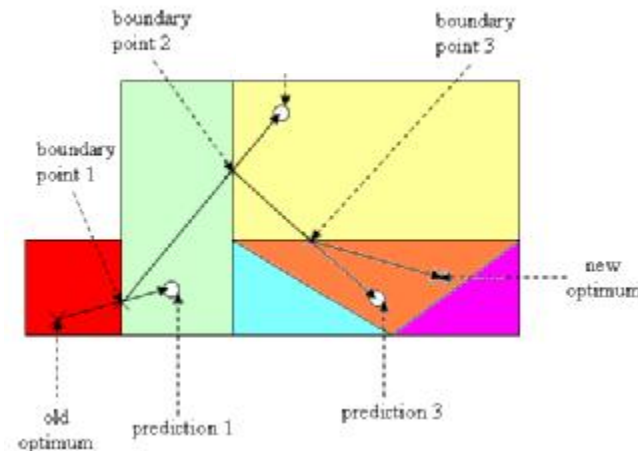
- $\text{rank } \mathbf{K}_{\text{BAL}} = n, n-1, n-2, \dots$



- For singular H

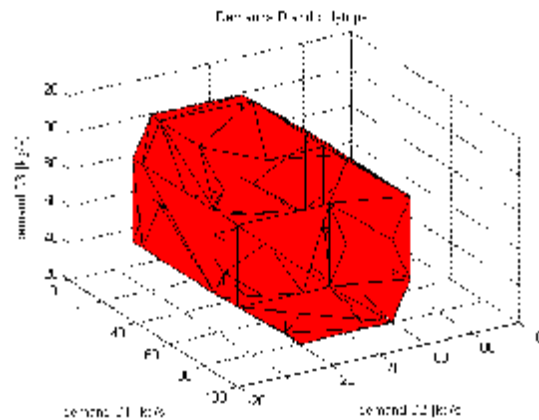
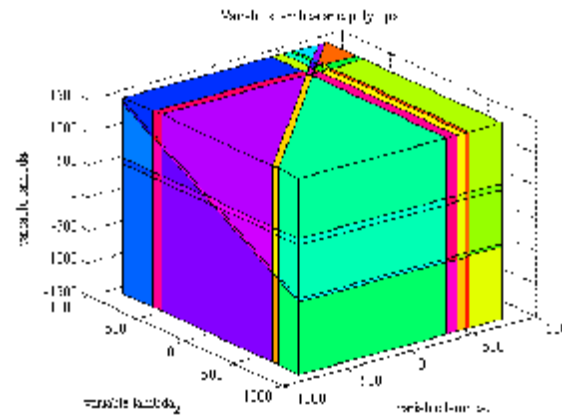
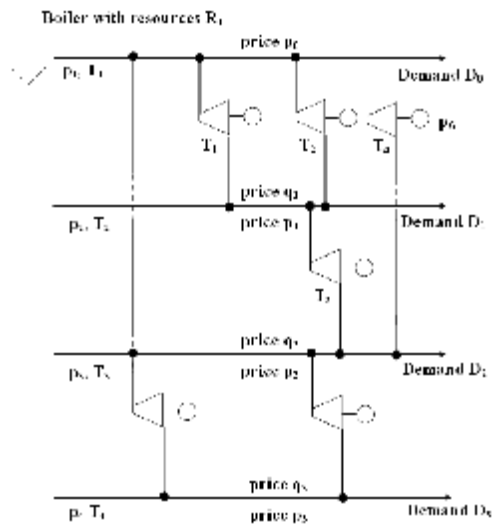
- no discoordination change on polytope boundary in D-space
- direction in λ -space given

$$\mathbf{K}_{\text{BAL}} \hat{\lambda} = 0$$



Example: comparison of the methods

- Max generation, given demand from individual headers
 - three headers
 - six backpressure/extraction turbines



Steam demand changes / number of iterations	Steepest descent [-]	Newton's method [-]		Sing. Hessian it.		Sum	Proposed method [-]
Starting demand: D0 = [70;40;50] (kg/s)	iteration	iteration	Subiterations				
Demand D1: [70 50 50]	77	2	36	0	38	2	2
Demand D2: [40 60 30]	31	5	90	0	95	4	4
Demand D3: [25 70 50]	109	3	54	67	124	3	3
Demand D4: [45 49 85]	128	3	54	52	109	3	3
Demand D5: [10 60 75]	95	3	54	48	105	3	3
Demand D6: [40 70 30]	151	3	54	66	123	3	3
Demand D7: [10 60 75]	97	4	72	66	142	3	3
Demand D8: [30 20 95]	26	3	54	48	105	3	3
Demand D9: [42 48 48]	92	3	54	48	105	3	3
Demand D10: [40 60 30]	27	1	18	0	19	1	1

Wireless control networks

- optimal node allocation
- communication issues

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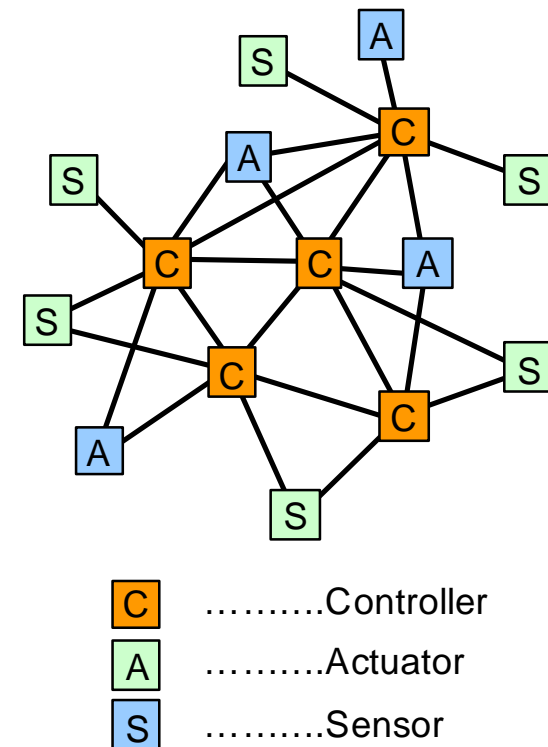
Optimization problem involving **distribution of control algorithms to a set of controllers in networked control system**. Each algorithm has certain computational load, needs to communicate with a set of sensors and/or controllers and has to be executed in certain number of instances.

Constraints:

- Computational power of controllers
- Links bandwidth
- Links quality

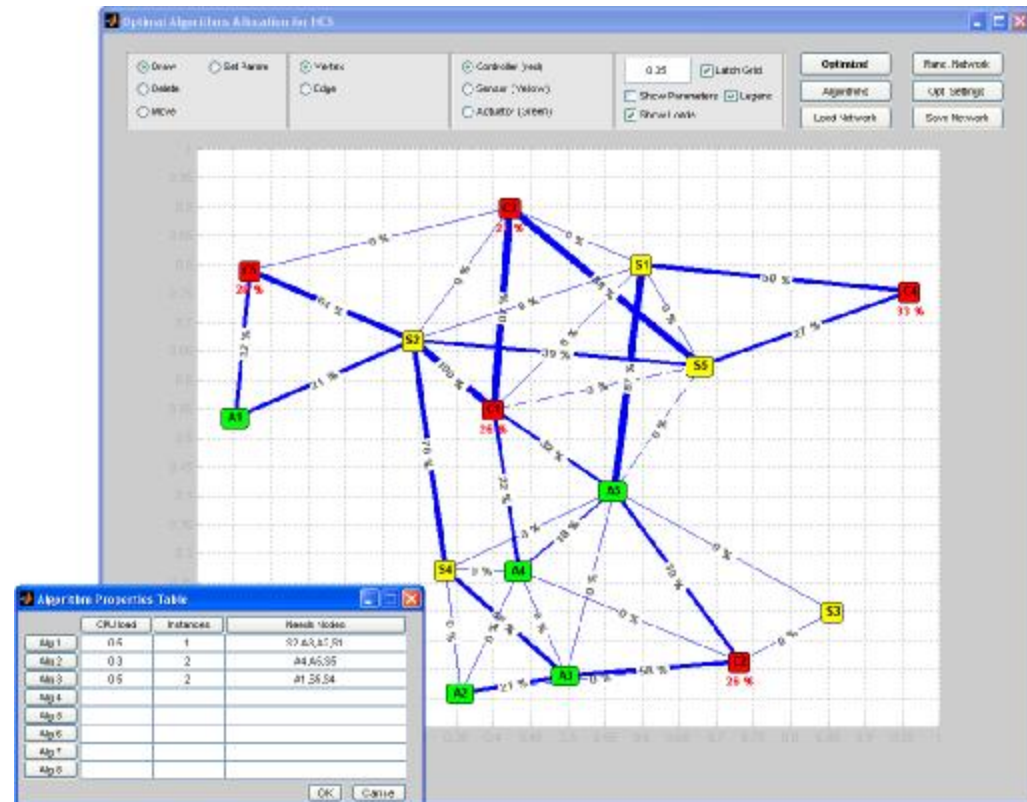
Considered Optimality:

- Minimization of hops between controllers and needed sensors and/or actuators
- Preference of high quality links
- Even distribution of CPU load
- Even distribution of communication traffic
- Robustness to link failure (without reallocation)
- Exclusion of links with quality below threshold



Algorithm

- Allocation algorithm was developed based on [linear/quadratic binary programming](#).
- It allows to incorporate all optimization criteria mentioned on previous slide while complying with resources constraints.
- Algorithm can be used for networks with up to several 10's of nodes -> it can be used as a reference solution for suboptimal algorithms able to cope with larger networks.
- Algorithm optimally allocates algorithms to controllers and also finds best communication paths.
- Issue: scalability

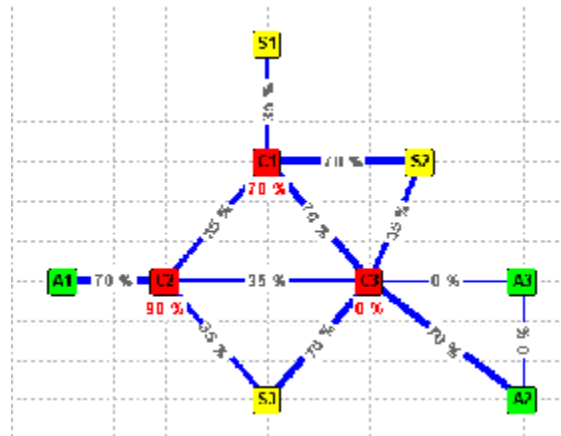


Small Scale Example

- 3 controllers, 3 sensors and 2 actuators
- Unit links bandwidths
- Unit controllers computing power
- Same links load for all algorithms = 35%

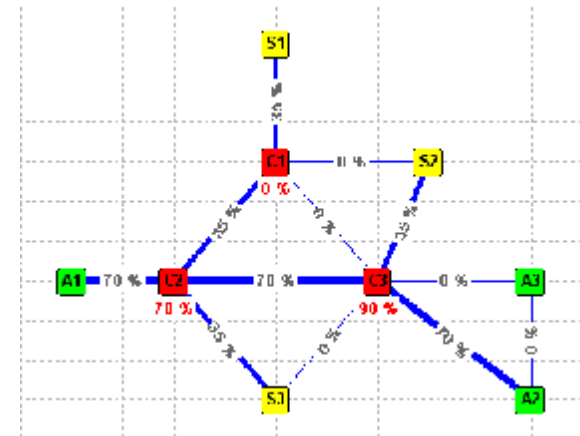
Alg.	Cont. load	Needs nodes
A1	50 %	S2,A2
A2	30 %	S1,S3,A2
A3	40 %	S3,A1
A4	40 %	S2,A1,A2

Feasible solution



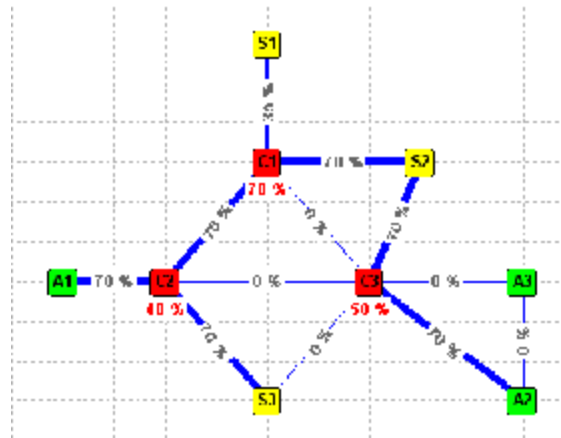
C1:(A2,A3), C2:(A1), C3:(A4)

Hops minimization



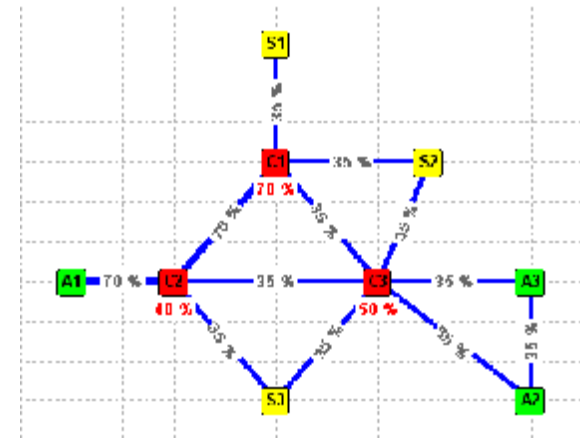
C1:(-), C2:(A3,A4), C3:(A1,A2)

Hops minimization & controllers load equalization



C1:(A2,A4), C2:(A4), C3:(A1)

Hops minimization & controllers and links load equalization



C1:(A2,A4), C2:(A4), C3:(A1)
(different routing to previous solution)

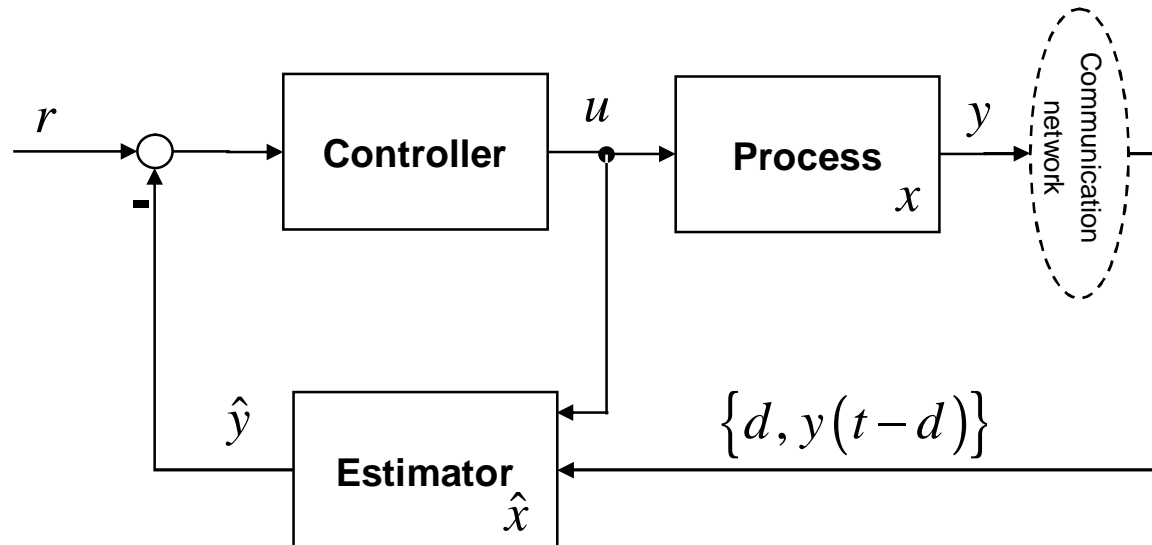
Compensation of communication delay

- **Using state estimator of augmented system for estimating current process output (SISO, MISO)**

- Kalman filter replacing Smith predictor
- added noise-cancelling and disturbance estimation capability

- **Several levels of complexity**

- Optimal KF, multiple data at a time
- Suboptimal KF, handling only the latest measurement
- **Approximated by a switched gain** (set of pre-computed gains in a look-up table)
- 1st/2nd order approximations



- **Solution – dynamically augmented KF**
 - tracking of missing samples
 - Bayesian insertion at “time of arrival” vs. Riccati formulation
- **Easy to verify**
 - DA KF with randomly delayed data
 - Standard Kalman filter (no delays)
 - States of both filters equal whenever all data available
- **Suboptimal solution**
 - Kalman gains calculated offline, gains stored in a look-up table
 - Direct analog of the time invariant Kalman filter
 - No second order statistics (covariance) need to be calculated
 - Scalable complexity – implemented as part of PID controller
- **Out-of-sequence MVs**
 - Dual problem