

Synthesis for Idle Speed Control of an Automotive Engine

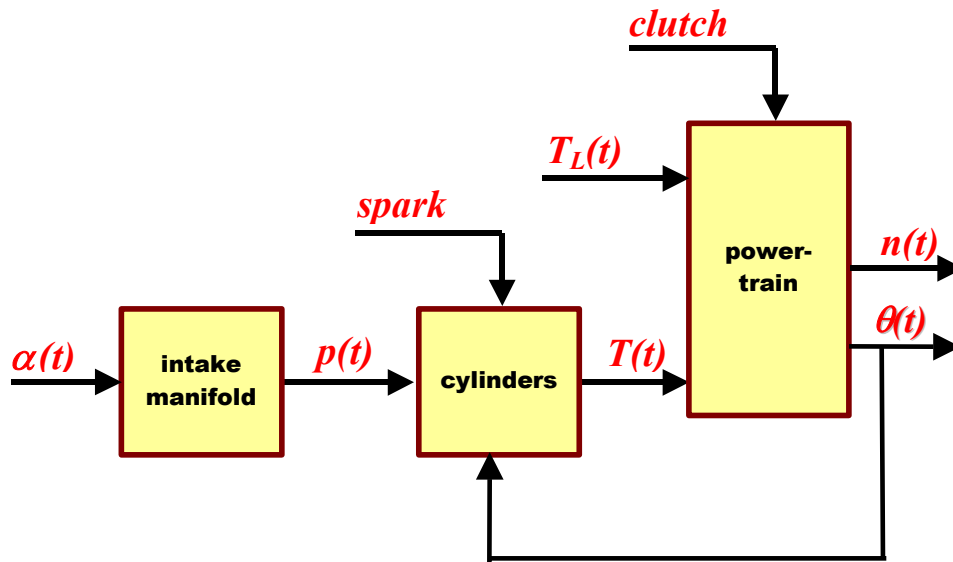
**A. Balluchi⁽¹⁾, F. Di Natale⁽¹⁾,
A. Sangiovanni-Vincentelli^(1,2) and J.H. van Schuppen⁽³⁾**

(1) PARADES GEIE, Rome, I

(2) Dept. of EECS., Univ. of California at Berkeley, CA

(3) CWI, Amsterdam, NL

“Idle Speed Control” Case Study

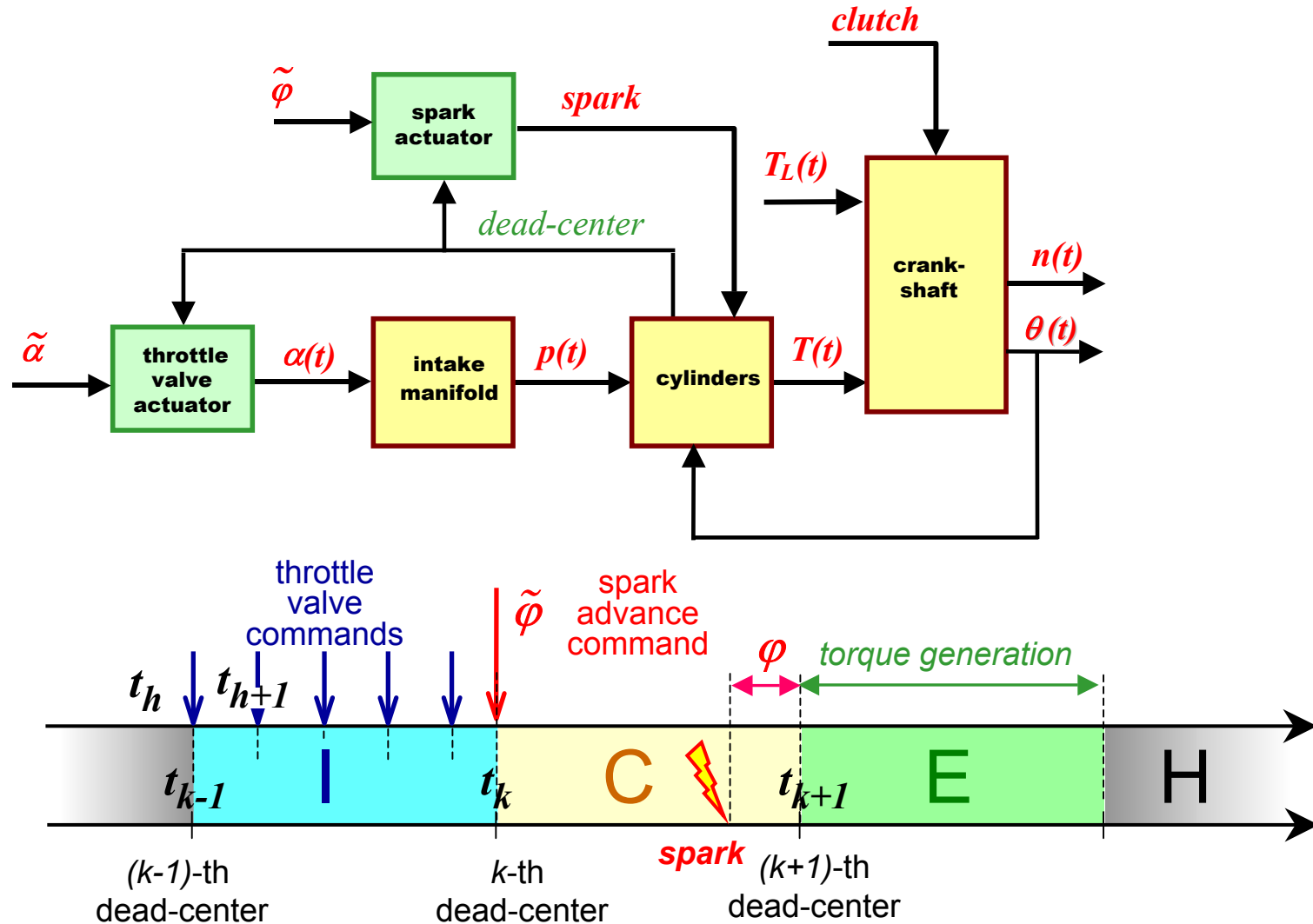


Control Problem

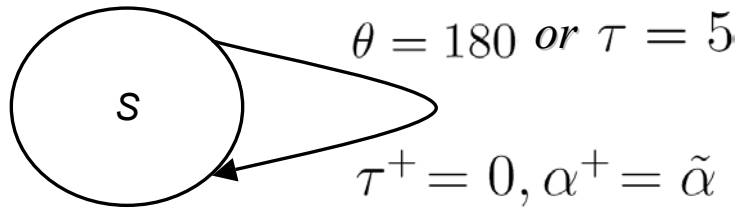
- Given a value of n_0 , Δ and T_L^M , determine whether there exist
- an ignition control *spark* and
 - a throttle control $\alpha(t)$
- that maintain the crankshaft speed $n(t)$ in the given range $n_0 \pm \Delta$ under
- any driver's action on *clutch* pedal,
 - any load torque $T_L(t)$ in $[0, T_L^M]$.

| Controls | Time / Value | Disturbances | Time / Value |
|-----------------------|--------------|----------------------|--------------|
| ignition <i>spark</i> | disc / disc | clutch <i>clutch</i> | disc / disc |
| throttle α | cont / cont | load torque T_L | cont / cont |

Throttle valve and spark ignition actuators

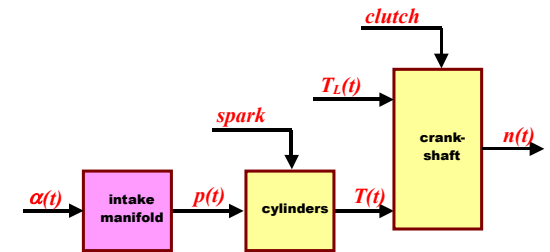


Throttle valve actuator and intake manifold model



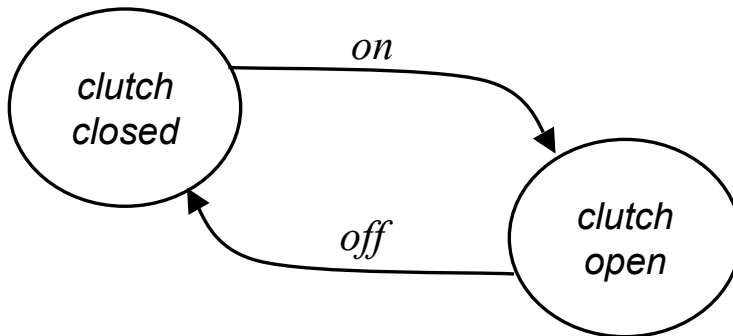
$$\dot{\tau} = 1000$$

$$\dot{p}(t) = a_p(p(t) - p_0) + b_p(\alpha(t) - \alpha_0)$$

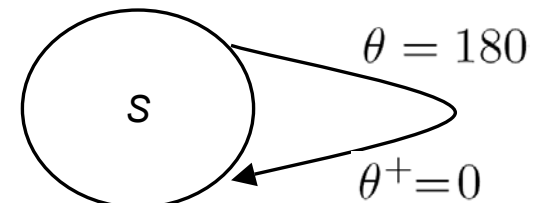
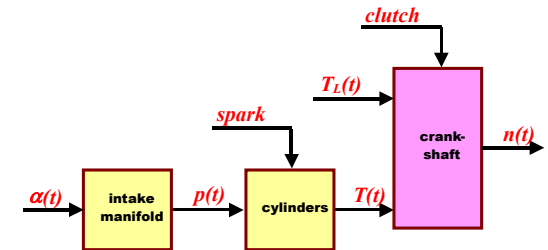


Crankshaft model

$$\dot{n}(t) = a_n^L n(t) + b_n^L [T(t) - \bar{T}_p - T_l(t)]$$

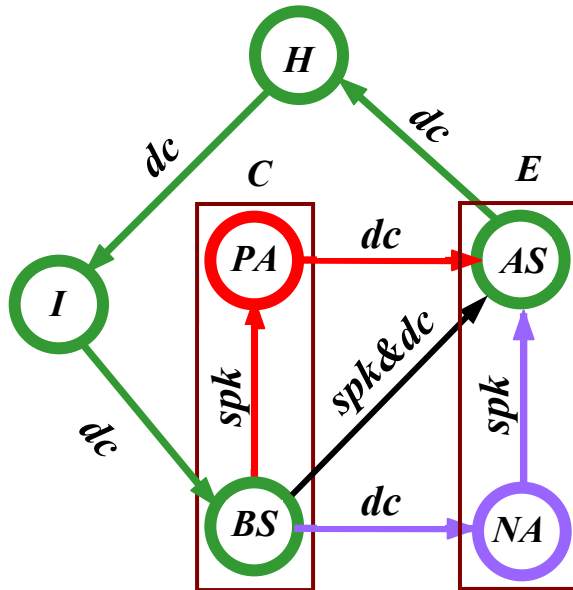


$$\dot{n}(t) = a_n n(t) + b_n [T(t) - T_p - T_l(t)]$$



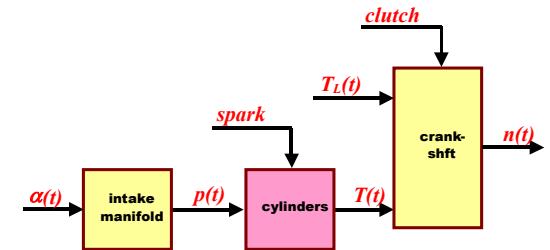
$$\dot{\theta}(t) = 6n(t)$$

Single cylinder FSM: engine cycle



positive spark advance

negative spark advance



$I \rightarrow BS$

$$m := f_m(p, n)$$

$$T_C := G^c f_m(p, n) + T_0^c$$

$C \rightarrow E$

$$T_C = 0$$

$BS \rightarrow PA$

$$\varphi := 180 - \theta$$

$C \rightarrow AS$

$$T_E := (G^e m + T_0^e) \eta(\varphi)$$

$NA \rightarrow AS$

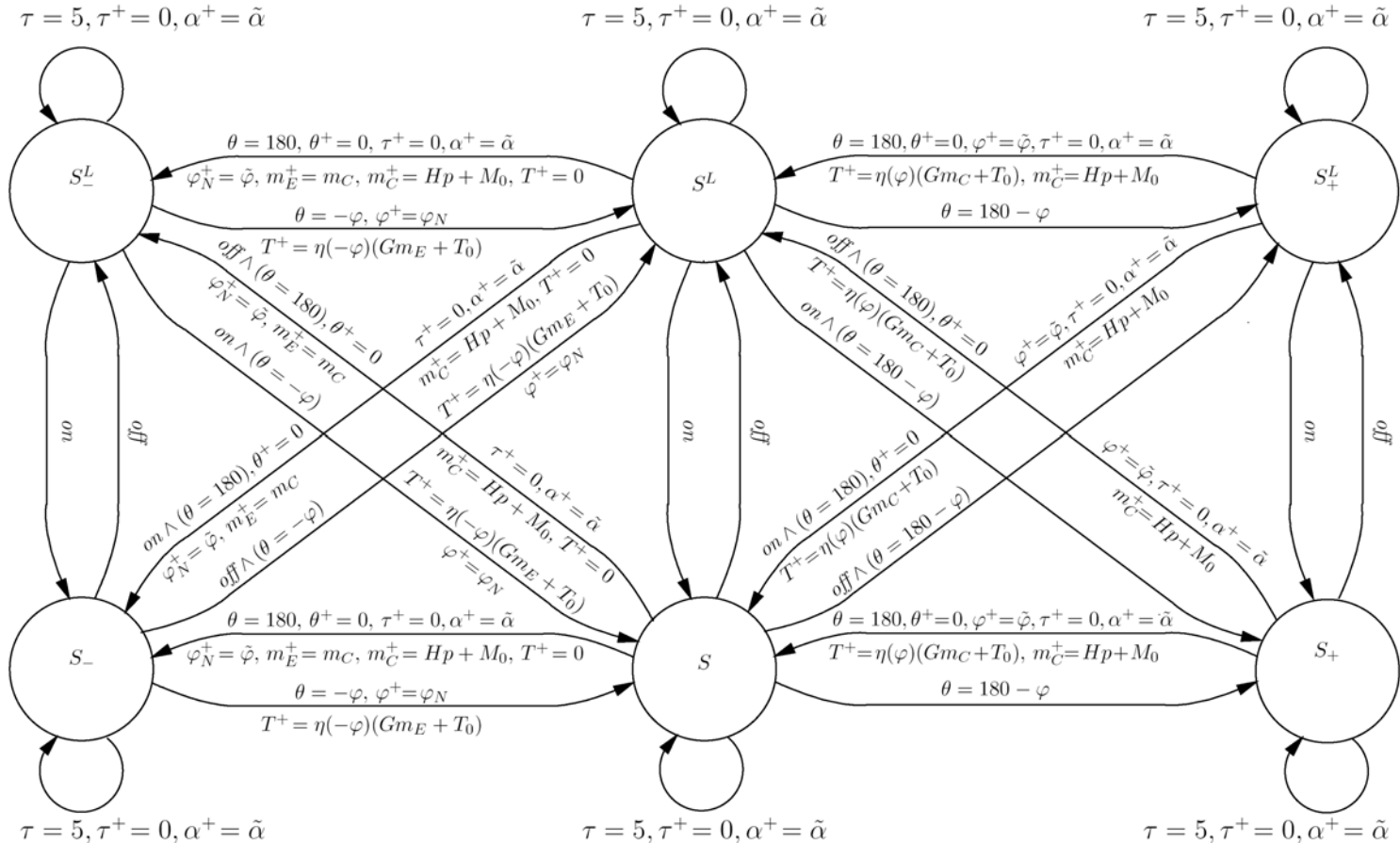
$$T_E := (G^e m + T_0^e) \eta(-\theta)$$

$AS \rightarrow H$

$$T_E = 0$$

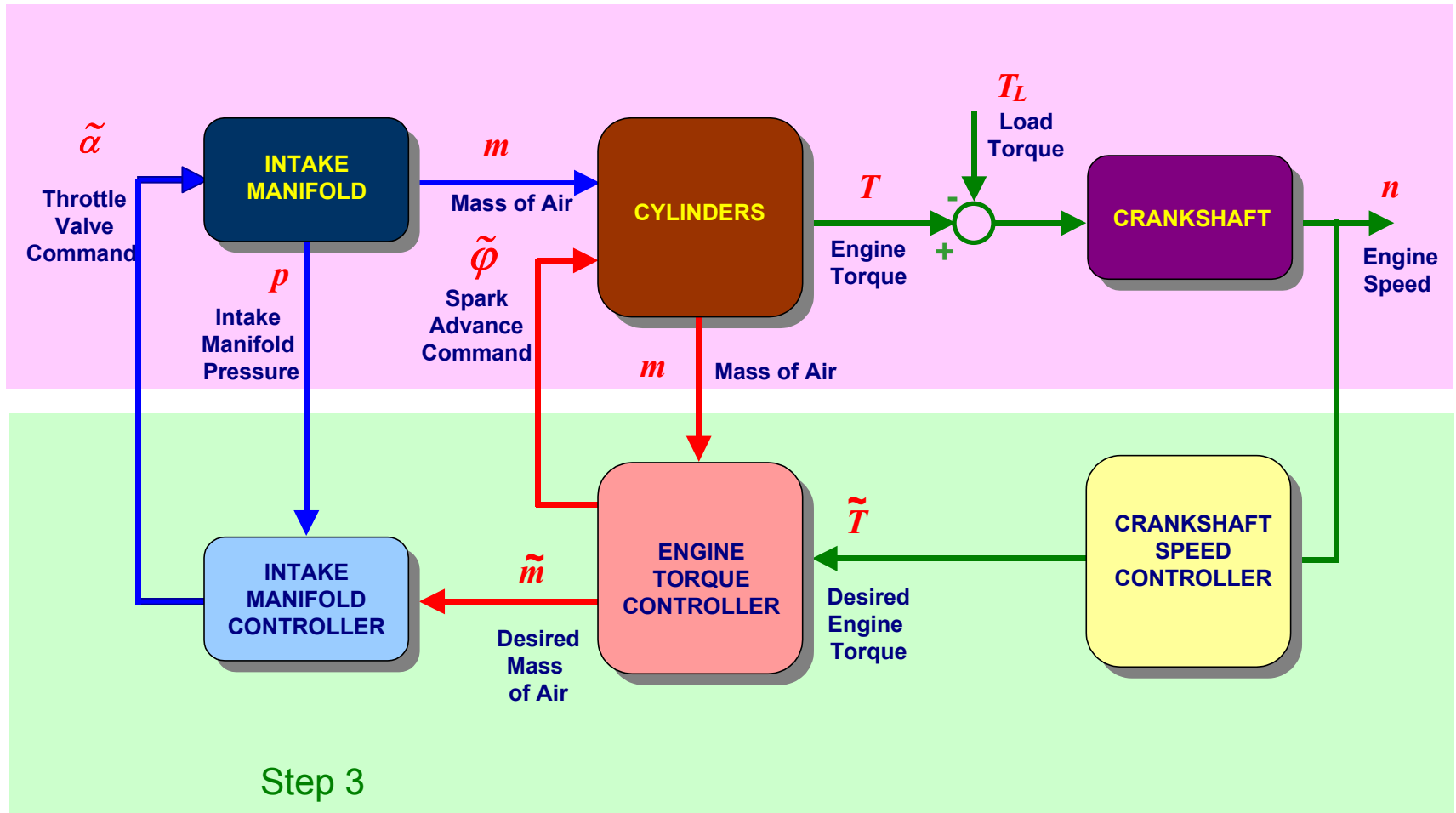
Piecewise-affine hybrid system model

$$\begin{aligned} \dot{\tau} &= 1000 & \dot{n}(t) &= a_n^L n(t) + b_n^L [T(t) - \bar{T}_p - T_l(t)] \\ \dot{p}(t) &= a_p(p(t) - p_0) + b_p(\alpha(t) - \alpha_0) & \dot{\theta}(t) &= 6n(t) \end{aligned}$$



$$\begin{aligned} \dot{\tau} &= 1000 & \dot{n}(t) &= a_n n(t) + b_n [T(t) - T_p - T_l(t)] \\ \dot{p}(t) &= a_p(p(t) - p_0) + b_p(\alpha(t) - \alpha_0) & \dot{\theta}(t) &= 6n(t) \end{aligned}$$

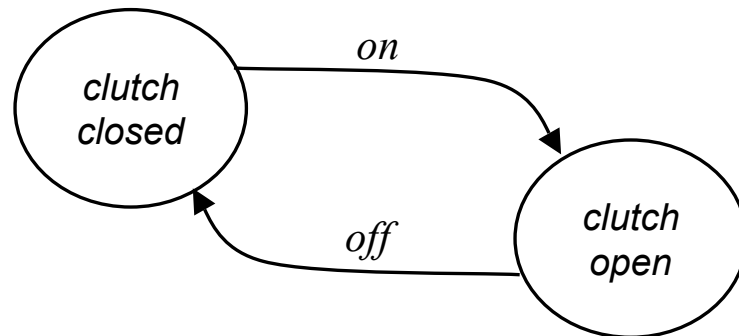
Idle Speed Controller Design



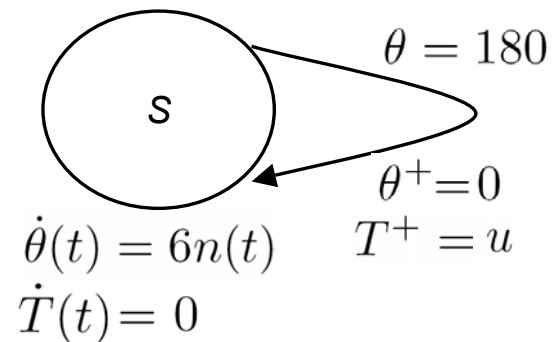
Step 1: Crankshaft speed controller

- ◆ Consider the crankshaft model with states (n, \mathcal{G}, T)

$$\dot{n}(t) = a_n^L n(t) + b_n^L [T(t) - \bar{T}_p - T_l(t)]$$

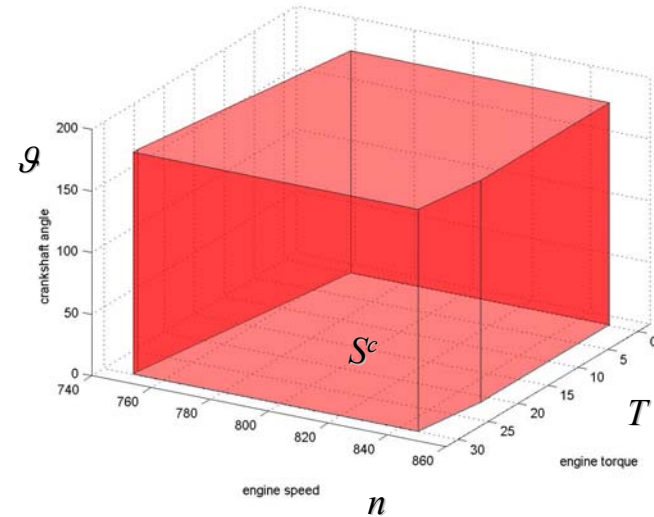
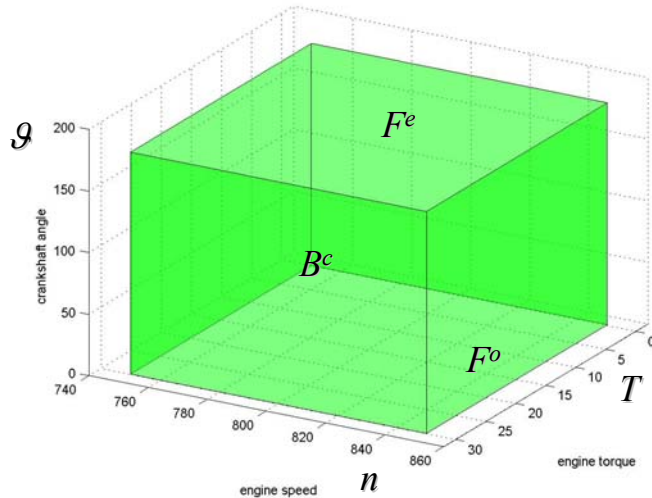


$$\dot{n}(t) = a_n n(t) + b_n [T(t) - T_p - T_l(t)]$$



- ◆ **Problem:** Find a control strategy for the resets of the engine torque T such that the crankshaft speed $n(t)$ is maintained bounded to $[750, 850]$.

Crankshaft speed constraint satisfaction



◆ Consider the state space (n, θ, T)

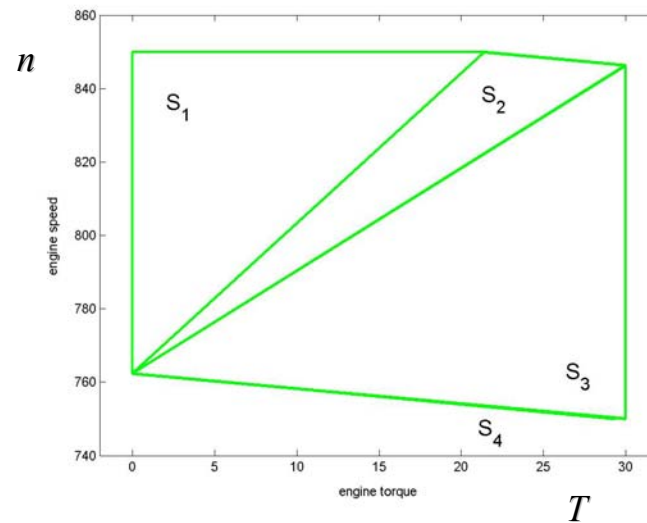
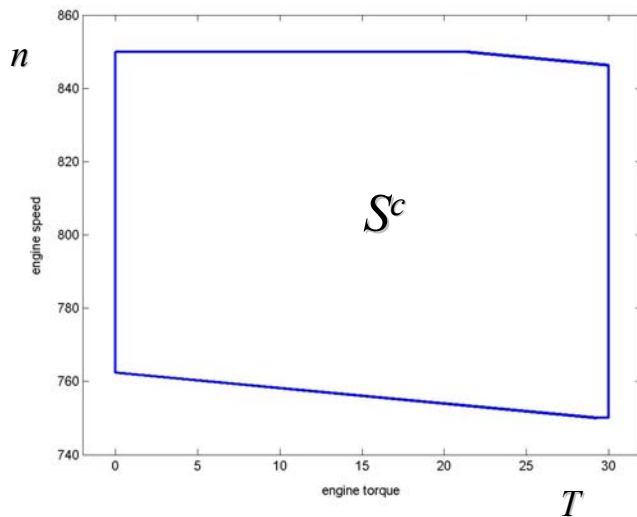
▲ If the exit facet from B^c is $\theta = 180$, then $n(t)$ belongs to $[750, 850]$ for $\theta: 0 \rightarrow 180$

▲ If (n_0, T_0) belongs to S^c , then $\theta = 180$ is the unique exit facet from B^c

◆ Hence,

▲ If at each dead-center (n, T) belongs to S^c , then $n(t)$ always belongs to $[750, 850]$.

Step 2: Engine torque controller



- ◆ **Problem:** find a robust controlled invariant set contained in S^c , for a model of the crankshaft evolution between dead-centers

$$n(k+1) = a_d(k)n(k) + b_d(k)(T(k) - T_p - T_l(k))$$

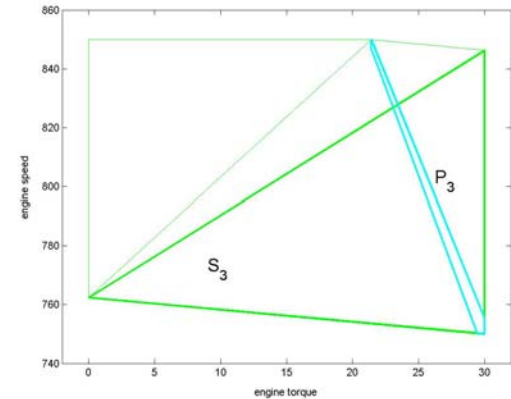
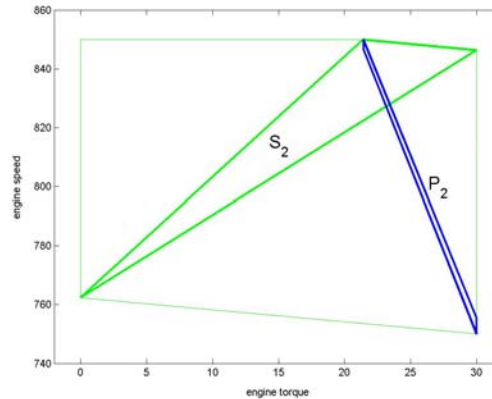
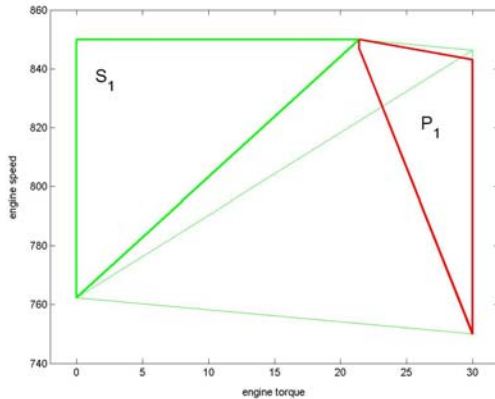
$$T(k+1) = u(k)$$

- ◆ Time-varying parameters represent dependence from dead-center times

$$a_d(k) = e^{a_n(t_{k+1}-t_k)}$$

$$b_d(k) = -[1 - e^{a_n(t_{k+1}-t_k)}]b_n/a_n$$

Robust invariance via triangularization



◆ Approach:

▲ S^c is partitioned in simplex: S_1, S_2, S_3 and S_4 .

▲ a feedback u is designed s.t. $S_1, S_2, S_3 \rightarrow S_2 \cup S_3$, i.e. $S_2 \cup S_3$ is a robust invariant set

$$u(k) = g_p(n(k), T(k)) = F_p \begin{bmatrix} n(k) \\ T(k) \end{bmatrix} + h_p \quad \text{for } (n, T) \text{ in } S_p$$

◆ Robustness with respect to

▼ Load torque disturbance, clutch disturbance, dead-center time and parameters uncertainties.

Implementation of the affine controller

- ◆ Feedback $u(k)$ is implemented in terms of engine torque $T = \eta(\varphi)(Gm + T_0)$

Since spark advance efficiency is bounded to the interval $[0.6, 1]$ then

$$0.6(Gm + T_0) \leq g_p(n, T) \leq (Gm + T_0) \quad \forall (n, T) \in S_1 \cup S_2 \cup S_3$$

- ◆ Air-fuel mixture mass is regulated to the interval $[m_{min}, m_{max}]$ with

$$m_{min} = \frac{1}{G} \left[\left(\max_{v_i \in S_1, S_2, S_3} F_p v_i + h_p \right) - T_0 \right], \quad m_{max} = \frac{1}{0.6} m_{min}$$

- ◆ Engine torque is controlled by the spark advance feedback $\tilde{\varphi} = \begin{cases} \phi_1 & \text{if } \phi_1 \geq 0 \\ \phi_2 & \text{if } \phi_1 < 0 \end{cases}$

$$\phi_1 = \eta^{-1} \left(\frac{F_p [n(t_k) \quad T(t_k)]^T + h_p}{Gm_C(t_k) + T_0} \right) \quad \text{positive spark advance}$$

$$\eta(\phi_2)(Gm_C(t_k) + T_0) = \frac{1 - e^{-\frac{30}{n(t_k)}}}{1 - e^{-\frac{30}{n(t_k)} \left(1 - \frac{\phi_2}{180}\right)}} \left[F_p \begin{pmatrix} n(t_k) \\ T(t_k) \end{pmatrix} + h_p \right] \quad \text{negative spark advance}$$

Step 3: Intake manifold controller

- ◆ A feedback $\alpha(k) = f_1 p(k) + h_1$ is designed to control p to the target interval

$$p_{min} = \frac{m_{min} - M_0}{H} \quad \text{and} \quad p_{max} = \frac{m_{max} - M_0}{H}$$

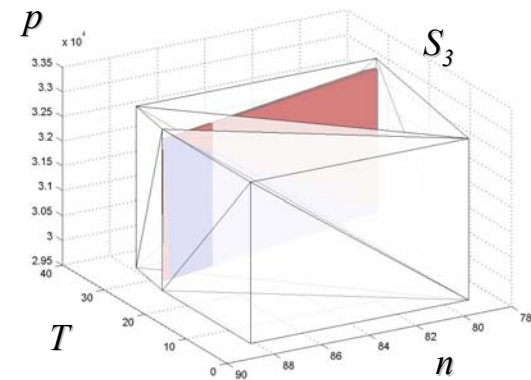
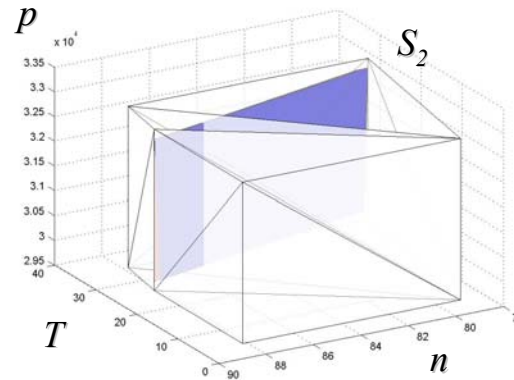
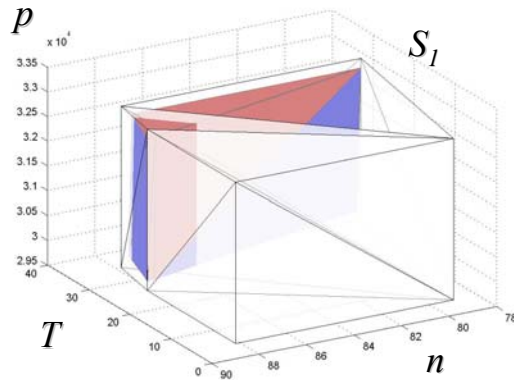
- ◆ The throttle valve feedback is implemented in the 5msec-sampling as follows

$$\alpha(t_h) = \frac{\bar{p}(k+1) - e^{a_p \tau} p(t_h) + (1 - e^{a_p \tau}) p_0 + [1 - e^{a_p \tau}] b_p / a_p \alpha_0}{-[1 - e^{a_p \tau}] b_p / a_p}$$

where $\tau = \frac{30}{n(t_h)} \left(1 - \frac{\theta}{180}\right)$ is the estimated time to the next dead-center and

$$\bar{p}(k+1) = e^{a_p \frac{30}{n(t_k)}} p(t_k) - \left[1 - e^{a_p \frac{30}{n(t_k)}}\right] \frac{b_p}{a_p} (f_1 p(t_k) + h_1)$$

Robust invariance for the closed loop system

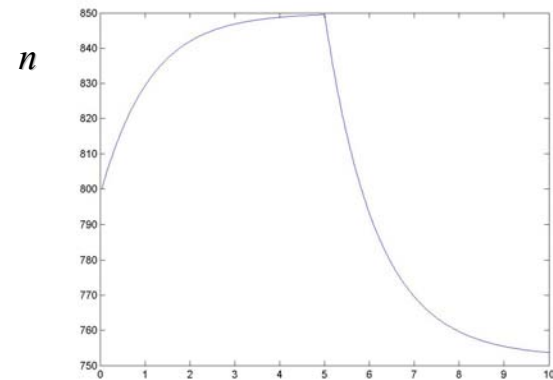
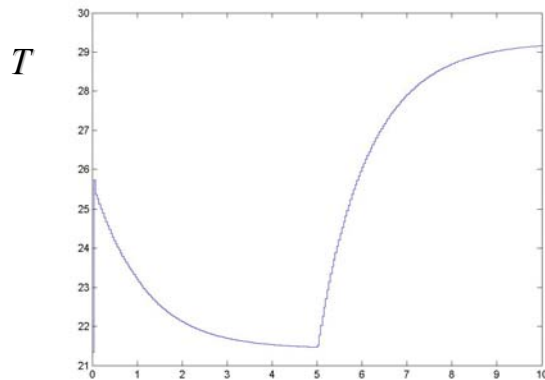
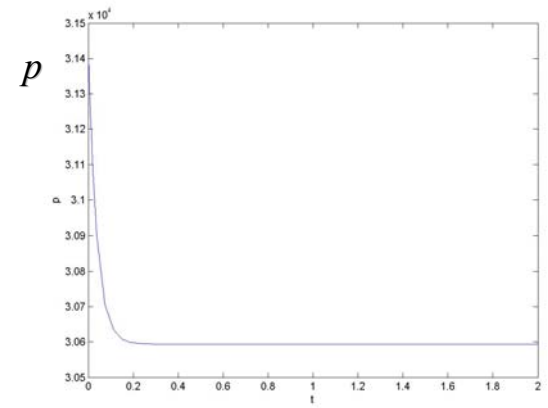
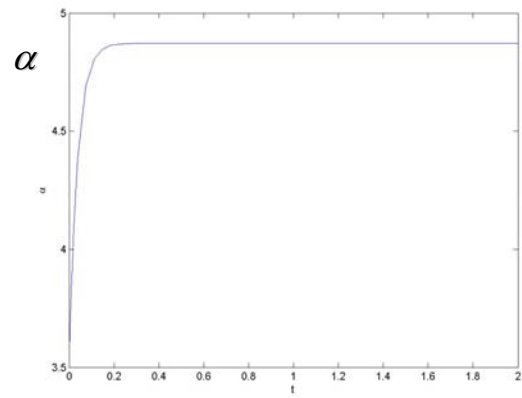
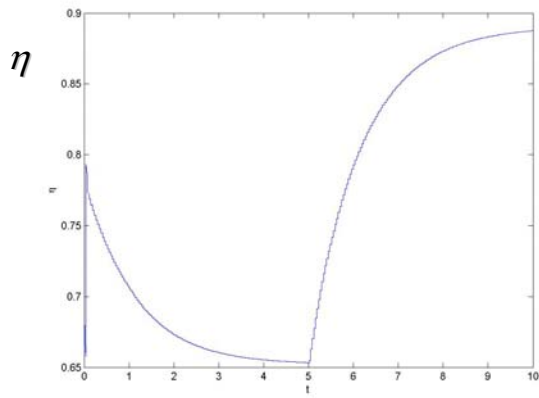


◆ Robust invariance of the computed subset of the state space, under

- ▲ Clutch and torque load disturbances
- ▲ Dead-center time interval length uncertainties
- ▲ Parameter uncertainties

for the closed-loop system obtained with the proposed controller has been verified.

Simulation results



Conclusion

- ◆ **Idle speed control has been formulated as an affine hybrid system control problem on polytopes.**
- ◆ **The approach to controller synthesis is a combination of**
 - ▲ **Back-stepping procedure and interactive design**
 - ▲ **Control for affine systems on polytopes**
 - ▲ **Theory of invariant sets**
- ◆ **Input and state constraints are handled by**
 - ▲ **Partitioning the space in polytopes**
 - ▲ **Designing feedback controls for each polytope such that the state of the closed loop system is driven only on those polytopes for which constraints are verified**
- ◆ **Future work: introducing performance specifications**